

## Diagonal reduction algebra and the reflection equation

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### Abstract

© 2017, Hebrew University of Jerusalem. We describe the diagonal reduction algebra  $D(\mathfrak{gl}\ n)$  of the Lie algebra  $\mathfrak{gl}\ n$  in the R-matrix formalism. As a byproduct we present two families of central elements and the braided bialgebra structure of  $D(\mathfrak{gl}\ n)$ .

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